Energy Minimization of Mobile Edge Computing Networks with Finite Retransmissions in the Finite Blocklength Regime

(Invited Paper)

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Abstract—We consider a mobile edge computing network supporting low-latency and ultra reliable services. Task offloading from the user to the edge server is operated under a truncated retransmission process, i.e., the allowed retransmission times are finite. For such network, we first characterize the end-to-end error probability and the total energy consumption. We subsequently provide a framework design allowing to determine the optimal number of allowed retransmissions and the blocklength for a single transmission/retransmission, where the objective is to minimize the expected total energy consumption while guaranteeing the end-to-end reliability. Via simulation, we confirm our analytical model and evaluated the system performance.

Keywords—edge computing, finite blocklength, offloading, retransmission

I. INTRODUCTION

Recently emerging mobile edge computing (MEC) technologies enable the flexible and rapid deployment of latency-critical closed-loop applications by offloading the computation process to the edge of networks [1]. This is motivated by much lower latencies compared to realizing the computation at the cloud. In addition to the low-latency aspect, the demand for ultra-reliability is another key concern in the design of MEC networks, e.g., to satisfy the requirement of online virtual reality gaming and vehicle edge computing applications. Moreover, note that achieving green communication has been one of the key strategies in the design of future networks. Hence, the future MEC networks are expected to guarantee reliable and low-latency services (including both communication and computation) for edge users, while consuming as little energy as possible.

Various energy-efficient offloading schemes have been studied for MEC networks [2]–[6]. In particular, [2] proposes a collaborative task execution algorithm with a partial offloading. The authors in [3] study a wireless powered scenario where the devices are charged by the MEC network and use the charged power to offload tasks. The work in [4] introduces a three-node partition offloading design by optimizing both the time allocation and power allocation. In addition, reference [5] provides a cooperative offloading design where the nodes are able to share the computation results with each other. Moreover, the trade-off between the communication energy cost and the computation energy cost in the task offloading is investigated in [6], following which the total energy consumption is minimized. However, the above works do not consider the critical applications that demand low latency. In particular, to model the communication, it is more accurate to incorporate finite blocklength (FBL) coding assumptions into the analysis when low-latency applications are considered [7]. In such FBL regime, the data transmission is no longer arbitrarily reliable, especially when the blocklength is short. To improve the reliability in the FBL regime, retransmission schemes are proposed in [8], [9] to improve the reliability of the communication with FBL codes. However, in a MEC network the end-to-end delay requirement of a task is fixed, which indicates that the total delay cost of the communication phase and the computation phase are limited. Generally, if the blocklength for each transmission/retransmission is relatively long, the allowed retransmission time is low. Moreover, if the transmission and retransmissions cost a relatively long time, then the remaining time for computation is short. Note that both retransmission times and computing time length significantly influences the total energy consumption of serving the task. It is interesting and challenging to have an optimal framework design to minimize the energy consumption while guaranteeing the reliability and latency requirement of the service. To the best of our knowledge, this problem has not been addressed in the literature.

In this work, we consider a MEC network with retransmission-supported task offloading and aim at minimizing the expected total energy consumption of the system. We propose a framework design by optimally allocating the time duration of the single transmission/retransmission. Furthermore, we determine the optimal number of maximal allowed retransmissions. To solve the optimization problem, we leverage the analytical results of the decomposed subproblems to reformulate the original problem as a mixed integer convex problem. Via simulation, we validate our analytical model and evaluate the impact of various setups on the network performance.

II. SYSTEM MODEL

We consider a simple MEC network with a user equipment (UE) and a MEC server. Comprehensive computing tasks that are periodically generated at the UE, are required to be computed at the MEC server, e.g., the UE could be a state estimator which continuously reports time-sensitive information to the MEC server. The estimator is required to provide a state estimate within a fixed time bound \( T \), i.e., the total communication and computation time costs of a task is limited by \( T \). In addition, due to the reliability requirement, the overall error probability of whole communication/offloading and computation process needs to be

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lower than a given threshold \( \varepsilon_{\text{tot, max}} \).

The system operates in a time-slotted fashion, where time is divided into frames of length \( T \) equivalent to the "end-to-end" delay constraint of the estimation task. Each frame includes a communication phase and a computation phase. In the communication phase, the UE transmits the server the data packet of a task with a size of \( d \) bits via the wireless link from the UE to the server. The channel of the link is assumed to experience quasi-static fading, where the channel gain is constant within a frame and varies from one frame to the next. Denote by \( z \) the channel gain of the link. Then, the signal-to-noise ratio (SNR) of the received data at the server is given by \( \gamma = \phi z P_{\text{ue}}/\sigma^2_s \), where \( P_{\text{ue}} \) denotes the transmit power of the UE, \( \phi \) is the channel pathloss and \( \sigma^2 \) represents the noise power.

Due to the impact of FBL, the transmission is possibly erroneous. A Negative Acknowledgement (NACK) with a fixed small data size of \( d_0 \) bits is sent to the UE within a fixed duration of \( t_k \). The transmit power of the NACK is denoted by \( P_c \). The error probability of decoding/detecting the NACK at the UE is denoted by \( v \). After successfully decoding the NACK, the UE retransmits the data packet till the server successfully decodes it or the maximal allowed retransmission attempts \( N \) is reached. Denote the length of a single transmission/retransmission by \( t \). We denote by \( T_S \) the time duration of one symbol. Therefore, the blocklength of the transmission is given by \( m = \frac{T_S}{t} \). In addition, the time length of the communication phase in a frame is \( (n+1)t \), corresponding to \( \frac{(n+1)t}{T_S} \) symbols, where \( n \) is the number of retransmissions, i.e., \( n \in \mathbb{N} = \{1, \ldots, N\} \). In particular, \( n = 0 \) represents the initial transmission and \( N = 0 \) indicates that no retransmission is allowed.

To guarantee the stringent delay constraint, resources of the edge node are reserved for the task-related computation of the UE, i.e., the server with an adjustable CPU frequency \( f \) is able to execute the task immediately after successfully decoding the data packet. It is assumed that the server is able to adjust the frequency \( f \) per frame via the dynamic frequency and voltage scaling (DVFS) technique [10], [11] to adapt to the requirement of current task while the maximal available CPU frequency is \( f_{\text{max}} \). We assume in the following that there is a fixed computational load of each estimation task of \( c \) computation steps, while the execution time \( t_c \) depends on the chosen frequency of the processor. Hence, the frequency is chosen according to \( f = c/t_c \) with \( 0 \leq f \leq f_{\text{max}} \).

III. CHARACTERIZATIONS OF END-TO-END ERROR PROBABILITY AND TOTAL ENERGY CONSUMPTION

A. End-to-Task Error Probability in FBL regime

With the fixed task data size \( d \) and the determined blocklength \( m \) of the \( n \)th retransmission \( n = 0 \) represents the initial transmission), the corresponding coding rate is \( r = \frac{d}{m} \). According to the FBL model in [7], the (block) error probability of the \( n \)th retransmission is

\[
\varepsilon = \mathcal{P}(\gamma, r, m) \approx Q\left(\sqrt{\frac{m}{V(\gamma)}}(C(\gamma) - r)\log_2 2\right),
\]

where \( C = \log_2(1 + \gamma) \) is the Shannon capacity. In addition, \( V \) is the channel dispersion between the UE and the server [12]. Under a complex AWGN channel, \( V = 1 - (1 + \gamma)^{-2} \).

Combining both the errors of data transmission and NACK decoding, we can determine the overall error probability in the following way.

Case \( N = 0 \): No retransmissions are planned. Therefore, the end-to-end error probability \( \varepsilon_{\text{tot}} \) is

\[
\varepsilon_{\text{tot}} = \varepsilon, \text{ for } N = 0.
\]

Case \( N \geq 1 \): Firstly, the error probability of the initial transmission \( (n = 0) \) is \( \varepsilon \). If the error occurs at \( n = 0 \) and the UE successfully decodes the NACK, the process of the \( 1 \)st retransmission starts. In particular, the decoding error at the server occurs at the \( n \)th retransmission if one of the following two events happen: (A). The UE decodes the NACK of the \((n-1)\)th retransmission wrongly (the server receives nothing in the \(n\)th retransmission) (B). The NACK is decoded successfully but the \(n\)th retransmission fails. We denote by \( P_v(n) \) the error probability of the \(n\)th retransmission resulting from the failure of decoding NACK at the UE and by \( P_e(n) \) the part resulting from the data transmission error. Clearly, we have \( P_v(1) = \varepsilon v \) and \( P_e(1) = \varepsilon^2 (1 - v) \). Similarly, for \( n \)th retransmission, we have \( P_v(n) = \sum_{k=1}^{n} \varepsilon^n (1 - v)^{n-k} v P_e(n) \). \( P_v(n) \) is the probability that all previous NACKs succeeded but all transmissions failed, i.e., \( P_v(n) = \varepsilon^n (1 - v)^n \varepsilon \). As a result, the end-to-end error probability for \( N \) maximal allowed retransmission attempts is given by

\[
\varepsilon_{\text{tot}} = P_v(N) + P_e(N)
\]

\[
= \sum_{n=1}^{N} \varepsilon^n (1 - v)^{(n-1)} v + \varepsilon^{(N+1)}(1 - v)^N, \text{ for } N \geq 1.
\]

B. Total Energy Consumption

The total energy consumption \( E_{\text{tot}} \) in a frame consists of three parts: energy consumption of the UE, energy consumption at the server for transmitting NACK \( E_k \) and the computation energy cost at the server \( E_c \). Clearly, \( E_k \), \( E_k \), \( E_c \) are influenced by the total retransmission attempts \( N \), which generally is a random variable in the range from 0 to \( N \). In the following, we discuss the expected/average value of the three factors contributing to the energy consumption over the distribution of \( n \).

1) Energy consumption of data (re)transmission: The expected energy consumption of the UE \( E_k \) depends on the error probability of NACK and the maximal number of retransmission attempts. Clearly, the expected energy consumption of either the initial transmission or a retransmission is given by \( E_{k, 0} = t_P E_k + E'_{ue} \), where \( E_{k, 0} \) is the constant energy consumption at the server for receiving a task (with a given data size). Note that the server sends a NACK if the received packet is incorrectly decoded, while the corresponding retransmission occurs if the NACK is successfully decoded. Moreover, the initial transmission is always carried out regardless of \( N \). Therefore, the expected energy consumption of the \((n+1)\)th retransmission depends on the error probability of the \(n\)th retransmission and the reliability of the \(n\)th NACK. Hence, we have

\[
E_k = E_{k, 0} + \varepsilon (1 - v) E_{k, 0} + \cdots + \varepsilon^N (1 - v)^N E_{k, 0}
\]

\[
= \sum_{n=0}^{N} \varepsilon^n (1 - v)^n E_{k, 0}.
\]

2) Energy consumption for sending NACK: Clearly, the energy cost for sending a NACK is given by \( E_{k, 0} = t_k P_s + E'_{ue} \), where \( E'_{ue} \) is the constant energy consumption
at the UE for receiving a NACK. If the initial transmission succeeds, no NACK needs to be sent, i.e., $E_{k} = 0$. The probability that the first NACK occurs equals to the error probability of the initial transmission. Hence, the expected energy consumption of the first NACK is $\varepsilon E_{k,0}$. Moreover, the second NACK occurs if the first two (re)transmissions fail while the previous NACK is detected successfully, i.e., with probability $\varepsilon E_{k,0}$. Similarly, the probability of $n^{th}$ NACK is $\varepsilon^{n+1}(1-v)^{n}$. Hence, the expected energy consumption $E_k$ in a frame for sending all NACKs is

$$E_k = \varepsilon E_{k,0} + \varepsilon^2(1-v)E_{k,0} + \ldots + \varepsilon^{N+1}(1-v)^{N}E_{k,0}$$

$$= \sum_{n=0}^{N} \varepsilon^{n+1}(1-v)^{n}E_{k,0}. \quad (5)$$

3) Computation energy consumption: The energy consumption of computation is generally proportional to the workloads and the CPU frequency. In this paper, we adopt the non-linear energy consumption model of computation introduced in [14], given by

$$E_c = \kappa f^2 = \kappa^3 t_c^{-2}, \quad (6)$$

where $\kappa$ is a constant related to the hardware architecture.

Noting that the computation proceeds immediately, once the input data is received and occupies the rest of the frame, the computation time $t_c$ depends on the number of retransmissions $n$. In particular, the duration of communication phase (including data transmission and NACK transmission) is $(n+1)t + n t_k$. Then, the remaining time for computation is given by

$$t_{c}^{(n)} = T - (n+1)t - nt_k.$$ 

Denote by $E_{c}^{(n)}$ the computation energy consumption in the case that the server decodes the task data successfully with $n+1$ times transmission attempts ($n = 0$ represents the initial transmission). Then, we have

$$E_{c}^{(n)} = \kappa c^3 \frac{1}{(T-(n+1)t-nt_k)^2}. \quad (7)$$

Clearly, the probability of $n = 0$ is $1 - \varepsilon$. In addition, the $n^{th}$ retransmission happens when the first $n$ attempts (initial transmission and $n-1$ retransmissions) fail and the corresponding $n$ times NACKs are incorrectly decoded while the $n^{th}$ retransmission is successful. Hence, the probability that $n^{th}$ retransmission happens and is successful, is given by $\varepsilon^n (1-v)^n (1-\varepsilon)$. Therefore, the expected energy consumption for computation is

$$E_{c} = (1-\varepsilon)E_{c}^{(0)} + \varepsilon(1-v)(1-\varepsilon)E_{c}^{(1)} + \ldots + \varepsilon^N(1-v)^N(1-\varepsilon)E_{c}^{(N)}$$

$$= E_{c}^{(0)} - \varepsilon^{N+1}(1-v)^NE_{c}^{(N)} + \sum_{n=1}^{N} \varepsilon^n(1-v)^n - \varepsilon^n(1-v)^{n-1}$$

$$\approx E_{c}^{(0)} + \sum_{n=1}^{N} \varepsilon^n(1-v)^n - E_{c}^{(n)} - E_{c}^{(n-1)}$$

$$= E_{c}^{(0)} + \varepsilon^n(1-v)^n - \varepsilon^n(1-v)^{n-1}$$

where the approximation in the last step is tight due to the following reason: Note that we consider ultra reliable scenarios, i.e., $\varepsilon \ll 1$ and $v \ll 1$ hold. Hence, we have

$$E_{c}^{(0)} = \kappa f^2 \geq \varepsilon^3 \approx \varepsilon^{N+1} \approx \varepsilon^{N} \varepsilon \approx \varepsilon^{N+1}(1-v)^NE_{c}(N).$$

So far, we have derived the expected energy consumptions for task transmission, NACK and computation. Combining these results, the expected total energy consumption $E_{tot}$ can be written as

$$E_{tot} = E_{t} + E_{k} + E_{c}. \quad (9)$$

IV. OPTIMAL FRAMEWORK DESIGN

In this section, we provide a framework design for optimally determining the time duration of a single transmission/retransmission $t$ and the maximal allowed retransmission times $N$.

A. Problem Statement

Our objective is to minimize expected total energy consumption $E_{tot}$ while guaranteeing the given reliability requirements. In particular, the server should have sufficient time $t_c$ to finish the task within the duration of the frame even in the worst-case scenario, where the task data is received after $N$ attempts of transmission and retransmissions. In addition, recall that the overall error probability needs to be lower than $\varepsilon_{tot,max}$. Therefore, the problem is formulated by

$$\begin{align*}
\text{minimize} & \quad E_{tot} \\
\text{subject to} & \quad (n+1)t + nt_k = T, \forall n \in N, \\
& \quad c + (N+1)t - Nt_k \leq T, \\
& \quad \varepsilon_{tot} \leq \varepsilon_{tot,max} \quad \text{for } N \in Z.
\end{align*}$$

(10a), (10b), (10c), (10d)

B. Optimal Solution

In this subsection, we solve problem (10) in the following way. We firstly decompose the original problem (10) into $N_{max}$ subproblems, where $N_{max}$ is the maximal value of $N$ which is feasible for the original problem. In addition, we derive $N_{max}$ which limits the total number of subproblems. Moreover, we characterize the subproblems and based on that, we reformulate the original problem to be a solvable integer convex problem.

1) Decomposition of problem (10): Since $N$ is a positive integer and upper-bounded by $N_{max}$, there exists $N_{max}$ possible outcomes with respect to the retransmission events of the frame. For a given $N \in \{0, 1, \ldots, N_{max}\}$, we have the following subproblem:

$$\begin{align*}
\text{minimize} & \quad E_{tot} \\
\text{subject to} & \quad (10b), (10c) \text{ and (10d)} \\
& \quad N \in Z.
\end{align*}$$

(11a), (11b)

2) Upper Bounds of $N_{max}$: Without the constraints, $N_{max}$ is an unbounded integer, resulting in infinite subproblems. However, the maximal number of retransmissions is restricted due to the limited computation power of the server. In particular, by combining the constraints (10b) and (10c), we obtain an upper bound for $N_{max}$

$$N_{max} \leq \left\lceil \frac{T - \frac{c}{f_{max}} - t}{t + t_k} \right\rceil, \quad \text{(12)}$$

where $\lceil \cdot \rceil$ is the floor function.

3) Optimal Solution of subproblem (11): For a given $N$, we have the following lemma to handle the subproblem.

Lemma 1. The total error probability $\varepsilon_{tot}$ is convex in the time length of a single transmission/retransmission $t$.  

1Note that to support a reliable transmission, the SNR of the link cannot be extremely low. Hence, the extreme low SNR cases with $\gamma \geq \gamma_{th} < 0$ dB are out of scope in this design, i.e., operating the system with such low SNR means just wasting the energy.
Hence, $E$ in a convex feasible set for the feasible regime. We thus have

$$
\text{Lemma 2. The total energy consumption } E_{\text{tot}} \text{ is convex in } t.
$$

Proof: Recall that $E_{\text{tot}}$ consists of three parts, i.e., $E_{\text{tot}} = E_i + E_k + E_c$. In the following, we prove the convexity of each part respectively.

We start with $E_i$ and have

$$
\frac{\partial^2 E_i}{\partial t^2} = P_{\text{tx}} \left( \frac{(1-v)A}{T_s} + \sum_{n=2}^{\infty} \frac{(1-v)^n(n-1)e^n(\frac{\partial E_i}{\partial m})^2}{+n^n-1(1-v)^nA} \right),
$$

where $A = \frac{\partial^2 E_i}{\partial t^2} + 2 \frac{\partial E_i}{\partial m}$. Clearly, $\frac{\partial^2 E_i}{\partial t^2} \geq 0$ if $A \geq 0$.

Note that $V \leq 1$, $m \geq 1$ and $m = \frac{1}{T_s}$. Hence, we have

$$
A = \frac{1}{T_s} \frac{\partial^2 E_i}{\partial m^2} + 2 \frac{\partial E_i}{\partial m} = \sqrt{m} \sqrt{(C-k/m)(C+k/m)^2} \geq \frac{3C+k}{4m^2} \geq B \quad \text{m}^{3},
$$

where $B = C^3m^3 + (C^2k - 3C)m^2 - (Ck^2 - 3k)m - k^3$ is a third degree polynomial with the greatest root $m = k/C$.

Since $\varepsilon < \varepsilon_{\text{max}} \ll 1$, it holds $C > \frac{5}{m}$ for the transmission. In other words, the polynomial B is always positive (negative) when the first derivative of B is positive (negative) in the feasible regime. We thus have

$$
\frac{\partial B}{\partial m} = 2C^2km - Ck^2 + 3k + 3Cm(C^2m - 3) \geq 2Ck^2 - Ck^2 + 3k + 3Cm(C^2m - 3) \geq 0.
$$

Hence, $B \geq 0$ holds. According to (17), $A \geq 0$ also holds. As a result, $\frac{\partial^2 E_i}{\partial t^2} \geq 0$, i.e., $E_i$ is convex in $t$.

Secondly, for $E_k$ we have

$$
\frac{\partial^2 E_k}{\partial t^2} = \frac{\partial^2 E_k}{\partial t^2} + \sum_{n=1}^{N} n(n-1)\varepsilon^n-2 \left( \frac{\partial E_k}{\partial t} \right)^2 + n\varepsilon^n-1 \frac{\partial^2 E_k}{\partial t^2}
$$

As shown in [13], $\frac{\partial^2 E_k}{\partial t^2} \geq 0$ holds. It is clear that $\frac{\partial^2 E_k}{\partial t^2} \geq 0$, which proves that $E_k$ is convex in $t$.

Finally, we study the convexity of $E_c$ regarding $t$.

The second order derivative of $E_c$ to $t$ is given in (13), where $D_1 = E_c(n) - \bar{E}_c(n-1)$, $D_2 = \frac{\partial E_c(n)}{\partial t} - \frac{\partial E_c(n-1)}{\partial t}$ and $D_3 = \frac{\partial^2 E_c(n)}{\partial t^2} - \frac{\partial^2 E_c(n-1)}{\partial t^2}$. As proven previously, $\varepsilon$ is a convex and monotonically decreasing function with respect to $t$, i.e., $\frac{\partial \varepsilon}{\partial t} < 0$ and $\frac{\partial^2 \varepsilon}{\partial t^2} \geq 0$. In particular, we have $\frac{\partial^2 E_c}{\partial t^2} = 6(T - t) - 4 \geq 0$. Therefore, all the terms besides $D_i/k, \forall i \in \{1, 2, 3\}$ in (13) are non-negative, i.e., to determine the convexity of $E_c$ is to determine the sign of $D_i(n)$.

For $D_i(n)$, we have

$$
D_1(n) = \frac{1}{(T(n+1))t-n_k)^2} - \frac{1}{(T(n)+1(N-1)t_k)^2} \geq \frac{1}{(T(n+1))t-n_k})^2} - \frac{1}{(T(n)+1(N-1)t_k)^2} = 0.
$$

Similarly, we can show that $D_i(n) \geq 0$ and $D_i(n) \geq 0$ also hold by exploiting $n+1 \geq n$ to carry out the inequality chains. As a result, we have $\frac{\partial^2 E_c}{\partial t^2} \geq 0$.

So far, we have proven that $E_i$, $E_k$ and $E_c$ are convex in $t$. As a result, $E_{\text{tot}} = E_i + E_k + E_c$ is also convex in $t$.

4) Reformulation of the original problem (10) : According to Lemma 1 and the upper bounds of $N_{\text{max}}$, we can reformulate the original problem as

$$
\text{minimize}_{t, N} \quad E_{\text{tot}}
$$

subject to $N \leq \left[ \frac{T - \frac{e_{\text{max}}}{t} - t}{t + n_k} \right],

(10b), (10c) \text{ and } (10d).

(20c)

With Lemma 1 and Lemma 2, the objective function and all constraints are either convex or linear. Hence problem (20) is a mixed integer convex problem, which can be solved efficiently [15].

V. NUMERICAL RESULTS

In this section, we provide our numerical results obtained via Monte Carlo simulation. In the simulation, we consider the following parameter setups: First, the data size of a task $d$ is set to 1200 bits. In addition, the distance of the transmission is set to 10 m, while adopting the path-loss model in [16], given by $PL = 17.0 + 40 \log_{10}(r)$ with 2.4 GHz carrier frequency, where $r = 15$ m is the distance between the UE and the server. Moreover, we set the length of the frame to $T = 50$ ms and the symbol length to $T_s = 0.04$ ms. Furthermore, we set the bandwidth to $B = 5$ Mhz, transmit power to $P_{\text{tx}} = 20$ dBm and noise power to $N = -174$ dBm. For the computation, we set the maximal CPU-frequency to $f_{\text{max}} = 3.5$ GHz and total required workload to $c = 20$ Mcycles. Finally, we consider for the maximal total error probability as $e_{\text{tot,max}} = 0.001$.

To start with, we evaluate the impact of $t$ on the energy consumption while considering different setups of $N$. As shown in Fig. 1(a), the overall energy consumption $E_{\text{tot}}$ is convex in $t$ for each setup of $N$, which confirms our
analytical model. In addition, it is shown that boosting $N$ increases the energy consumption. However, as $N$ grows, the increment of $E_{\text{tot}}$ becomes smaller.

Secondly, by considering different setups of $T$ and $r$, the convexity of $E_{\text{tot}}$ in $t$ is further confirmed in Fig. 1(b) where curves of $r = 15$ m have only feasible values (due to the reliability constraint) when $t > 20$ ms. In addition to the convexity, we observe that a relatively shorter $T$, i.e., a more strict delay constraint, enhances the sharpness of the convexity. Moreover, a longer transmission distance, i.e., corresponding to a lower average channel SNR, significantly increases the energy consumption.

Finally, in Fig. 1(c), we present the minimized total energy consumption $E^*_{\text{tot}}$ and corresponding optimal transmission duration $t^*$ versus the target error probability $\varepsilon_{\text{tot, max}}$. In addition, the optimal solution of allowed transmission attempts $N^*$ is also shown in the plot. The figure reveals that for stringent $\varepsilon_{\text{tot, max}}$, it requires a sufficiently long transmission duration $t^*$, resulting in a higher energy consumption. Moreover, the dash line implies the optimal $N^* = 2$ and the solid line represents the optimal $N^* = 3$. It can be intuitively interpreted from the perspective of the computing energy consumption: if the target error probability is high, the system prefers a short transmission duration, such that both the computation energy consumption and the communication energy consumption are low. To compromise the relatively higher error probability caused by the short blocklength, the system offers more retransmission attempts. On the other hand, if the target error probability is low, given channel quality, the system is excepted to have a longer transmission duration to guarantee the reliability. Meanwhile, to maintain a low energy consumption, the length of the computation phase cannot be too short. As a result, the allowed retransmission attempts are reduced.

VI. CONCLUSION

We studied an edge computing network with a retransmission process. We provided an optimal framework design by optimally allocating the time duration of a single (re)transmission and determining the maximal allowed retransmission times, while the objective is to minimize the expected total energy consumption. By decomposing the original problem and characterizing the obtained subproblems, we gain insights on the design. Following these insights, we reformulated the original problem to be a solvable integer convex problem. Via simulation, we confirmed our analytical model and evaluated the system performance.

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